Data Structures and Algor nal Linguistics III (IGCL-RA-07)

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A tree is a set of nodes organ hierarchically with the follow

Definitions

- hierarchical properties:
- If a tree is non-empty, it has a
- If a tree is non-empty, it has a special node root
 Except the root node, every node in the tree has a unique parent (al nodes except the root are children of another node)
- Alternatively, we can define a tre-recursively:
- The empty set of nodes is a tree
 Otherwise a tree contains a root
 with sub-trees as its children



Binary trees

More definitions

Why study trees

* The nodes with the same parent are called siblings The nodes with children are called internal nodes

. A tree is a hierarchical non-linear data structure useful in n \ast We have already resorted to descriptions using trees (e.g., recursion trace)

A Tree is a graph with certain properties
It is also very common in (computational) linguistics:
Pare these representing syntactic structure of sentences
Language trees: representing the historical relations between languages
Decision trees a well-known algorithm for machine learning, also used for many NLT problems

- . The nodes without children are the leaf nodes
- · A path is a sequence of connected nodes
- . A node is the descendant of its ancestors
- . The subtree is a tree rooted by a non-root node
- . The height of a tree is the height of its root

. Binary trees where nodes can have at most two children, have many applications Binary trees have a natural order, each child is either



Ordered trees

- A tree is ordered if there is an ordering between siblings. Typical examples include:
 - A tree representing a document (e.g., HTML) structure
 Parse trees
 (maybe) a family tree
- . In many cases order is not important
 - Class hierarchy in a object-oriented prog
 The tree representing files in a computer

In a complete binary tree, every level except possibly the last, is completely filled, and all nodes at the last level is at the left

A perfect binary tree is a full binary tree whose leaf nodes have the same depth

a left child or a right child A binary tree is proper, or full if every node has either two children or none



Some properties of binary trees

For a binary tree with n_g leaf, n_1 internal, nnodes and with height h• $h+1 \le n \le 2^{h+1}-1$

- $\bullet \ 1\leqslant n_{g}\leqslant 2^{h}$
 - $\bullet \ h\leqslant n_i\leqslant 2^h-1$
 - $log(n+1)-1 \leqslant h \leqslant n-1$
 - For any proper binary tree, $n_{\ell} = n_{\perp} + 1$



Binary tree example: expression trees



Implementation of trees





Implementation of trees

- . Binary trees can also be implemented with arrays
- the root node is stored at index 0
 the left child of the node at index 1 is stored at 2i + 1
 the right child of the node at index i is stored at 2i + 2
 the parent of the node at index i is stored at 2i + 2
 the parent of the node at index i is at index [[i 1]/2]

 - . If the binary tree is complete, this representation



Breadth first traversal (level order)



queue = [] queue.append(root) while queue: node = queue.pop(0) # process the node print(node.data) for child im node.children: queue.append(child)

Pre-order traversal radebfcghijk

def pre_order(node) print(node.data) for child in node.children: pre_order(child)

