

inter Semester 2022/20 3 / 1



## More definitions

- · Two edges are parallel if their both endpoints
- are the same • For a directed graph parallel edges are ones with the same direction
- with the same direction • A self-loop is an edge from a node to itself
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   A path is an sequence of alternating edges and nodes
- A cycle is a path that starts and ends at the same node
- A path or a cycle is a simple if every node or the path is visited only once

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Nation Researcher 2022 (2) X / 1

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- A node X is reachable from another (Y) if there is a (directed) path from Y to X
- A graph is connected if all nodes are reachable from each other
- + A directed graph is strongly connected if all nodes are reachable from each other
- A subgraph a graph formed by a subset of nodes and edges of a graph
- If a graph is not connected, the max connected subgraphs are called the connected components

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- graph
- · A tree is a connected graph without cycles
- · A spanning tree is a spanning subgraph which is a tree
- · A forest is a disc cted acyclic graph

# Some properties

+ For an undirected graph with m edges and set of nodes V

$$\sum_{v \in V} deg(v) = 2\pi$$

- + All edges are counted twice for each node they are incident to
- + The total contribution of each node is twice its degree
- + For a directed graph with m edges and set of nodes V

$$\sum_{v \in V} indeg(v) = \sum_{v \in V} outdeg(v) = r$$



- · A spanning subgraph of a graph is a subgraph that includes all nodes of the graph
- · A tree is a connected graph without cycles
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# Some properties

- · For a simple undirected graph with n nodes and m edges
  - $m \leq \frac{n(n-1)}{2}$
  - If the graph is simple
  - the set of the se
    - $2m \leq n(n-1) \rightarrow m \leq \frac{n(n-1)}{2}$
  - . For a directed graph with n nodes and m edges  $m\leqslant n(n-1)$







# · A path is an sequence of alternating edges





