

Finite state transducers

Data Structures and Algorithms for Computational Linguistics III
(ISCL-BA-07)

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Finite state transducers

A quick introduction

- A *finite state transducer* (FST) is a finite state machine where transitions are conditioned on pairs of symbols
- The machine moves between the states based on an *input* symbol, while it outputs the corresponding *output* symbol
- An FST encodes a *relation*, a mapping from a set to another
- The relation defined by an FST is called a *regular* (or *rational*) relation



Introduction Operations on FSTs Decomposing FSTs Summary

Formal definition

A finite state transducer is a tuple $(\Sigma_i, \Sigma_o, Q, q_0, F, \Delta)$
 Σ_i is the *input* alphabet
 Σ_o is the *output* alphabet
 Q a finite set of states
 q_0 is the start state, $q_0 \in Q$
 F is the set of accepting states, $F \subseteq Q$
 Δ is a relation $(\Delta: Q \times \Sigma_i \rightarrow Q \times \Sigma_o)$

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Where do we use FSTs?

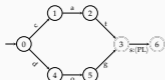
Uses in NLP/CL

- Morphological analysis
- Spelling correction
- Transliteration
- Speech recognition
- Grapheme-to-phoneme mapping
- Normalization
- Tokenization
- POS tagging (not typical, but done)
- partial parsing / chunking
- ...

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Where do we use FSTs?

example 1: morphological analysis

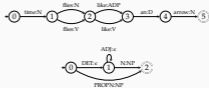


In this lecture, we treat an FSA as a simple PST that outputs its input: the edge label 'a' is a shorthand for 'aa'.

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Where do we use FSTs?

example 2: POS tagging / shallow parsing



Note: (1) It is important to express the ambiguity. (2) This gets interesting if we can 'compose' these automata.

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Closure properties of FSTs

Like FSA, FSTs are closed under some operations.

- Concatenation
- Kleene star
- Complement**
- Reversal
- Union
- Intersection**
- Inversion*
- Composition*

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FST inversion

- Since an FST encodes a relation, it can be reversed
- Inverse of an FST swaps the input symbols with output symbols
- We indicate inverse of an FST M with M^{-1}



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FST composition

sequential application



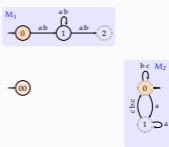
$M_1 \circ M_2$

aa	$M_{1,1}$	$M_{2,1}$	bb
bb	$M_{1,2}$	\emptyset	$M_{2,2}$
aaaa	$M_{1,1}$	$M_{2,1}$	baac
abaa	$M_{1,2}$	$M_{2,2}$	bbac

• Can we compose two FSTs without running them sequentially?

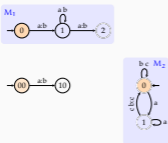
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FST composition

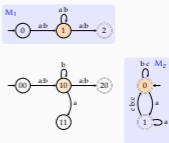


Introduction Operations on FSTs Decomposing FSTs Summary

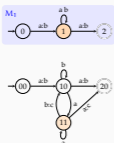
FST composition



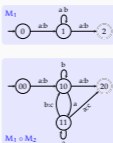
FST composition



FST composition



FST composition



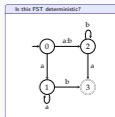
Projection

- Projection turns an FST into a FSA, accepting either the input language or the output language



FST determinization

- A deterministic FST has unambiguous transitions from every state on any input symbol
- We can extend the subset construction to FSTs
- Determinization of FSTs means converting to a subsequential FST
- However, not all FSTs can be determinized



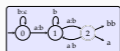
Sequential FSTs

- A sequential FST has a single transition from each state on every input symbol
- Output symbols can be strings, as well as ϵ
- The recognition is linear in the length of input
- However, sequential FSTs do not allow ambiguity



Subsequential FSTs

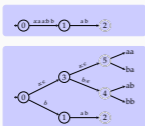
- A k -subsequential FST is a sequential FST which can output up to k strings at an accepting state
- Subsequential transducers allow limited ambiguity
- Recognition time is still linear



- The 2-subsequential FST above maps every string it accepts to two strings, e.g.,
 - $baa \rightarrow bba$
 - $baa \rightarrow bbbb$

An exercise

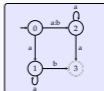
Convert the following FST to a subsequential FST



Determinizing FSTs

Another example

Can you convert the following FST to a subsequential FST?



Note that we cannot 'determine' the output on first input, until reaching the final input.

FSA vs FST

- FSA are acceptors, FSTs are transducers
- FSA accept or reject their input, FSTs produce output(s) for the inputs they accept
- FSA define sets, FSTs define relations between sets
- FSTs share many properties of FSAs. However,
 - FSTs are not closed under intersection and complement
 - We can compose (and invert) the FSTs
 - Determinizing FSTs is not always possible
- Both FSA and FSTs can be weighted (not covered in this course)

Next:

- Parsing

References / additional reading material

- jurafsky2009
- Additional references include:
 - roche1996; roche1997: FSTs and their use in NLP
 - mohri2009: weighted FSTs

